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Linear inequalities

A LEVEL LINKS

Scheme of work: 1d. Inequalities – linear and quadratic (including graphical solutions)

Key points

- Solving linear inequalities uses similar methods to those for solving linear equations.
- When you multiply or divide an inequality by a negative number you need to reverse the inequality sign, e.g. < becomes >.

Examples

Example 1 Solve $-8 \le 4x < 16$

$-8 \le 4x < 16$	Divide all three terms by 4.
$-2 \leq x < 4$	

Example 2 Solve $4 \le 5x < 10$

$4 \le 5x < 10$	Divide all three terms by 5.
$\frac{4}{5} \le x < 2$	

Example 3 Solve 2x - 5 < 7

$\begin{vmatrix} 2x-5 < 7 \\ 2x < 12 \\ x < 6 \end{vmatrix}$ 1 Add 5 to both sides. 2 Divide both sides by 2.		 Add 5 to both sides. Divide both sides by 2.
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Example 4 Solve $2 - 5x \ge -8$

$2-5x \ge -8$ $-5x \ge -10$ $x \le 2$	 Subtract 2 from both sides. Divide both sides by -5. Remember to reverse the inequality when dividing by a negative number.
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Example 5 Solve 4(x - 2) > 3(9 - x)

4(x-2) > 3(9-x) 4x-8 > 27 - 3x 7x-8 > 27 7x > 35 x > 5	 Expand the brackets. Add 3x to both sides. Add 8 to both sides. Divide both sides by 7.
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Practice

1	Sol	ve these inequalities.				
	a	4 <i>x</i> > 16	b	$5x-7 \le 3$	c	$1 \ge 3x + 4$
	d	5 - 2x < 12	e	$\frac{x}{2} \ge 5$	f	$8 < 3 - \frac{x}{3}$
2	Sol	ve these inequalities.				
	a	$\frac{x}{5} < -4$	b	$10 \ge 2x + 3$	c	7 - 3x > -5
3	Sol	lve				
	a	$2 - 4x \ge 18$	b	$3 \le 7x + 10 < 45$	c	$6-2x \ge 4$
	d	4x + 17 < 2 - x	e	4-5x<-3x	f	$-4x \ge 24$
4	Sol	ve these inequalities.				
	a	3t + 1 < t + 6		b $2(3n-1)$	$) \ge n +$	5
5	Sol	ve.				
		3(2-x) > 2(4-x) +	- 4	b $5(4-x)$	> 3(5 -	(-x) + 2

Extend

6 Find the set of values of x for which 2x + 1 > 11 and 4x - 2 > 16 - 2x.



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Answers

1	a	<i>x</i> > 4	b	$x \leq 2$	c	$x \leq -1$
	d	$x > -\frac{7}{2}$	e	$x \ge 10$	f	<i>x</i> < -15
2	a	<i>x</i> < -20	b	$x \leq 3.5$	с	<i>x</i> < 4
3	a	$x \le -4$ $x < -3$	b	$-1 \le x < 5$	c	$x \le 1$ $x \le -6$
	d	<i>x</i> < –3	e	x > 2	f	$x \le -6$
4	a	$t < \frac{5}{2}$	b	$n \ge \frac{7}{5}$		
5	a	<i>x</i> < -6	b	$x < \frac{3}{2}$		

6 x > 5 (which also satisfies x > 3)

