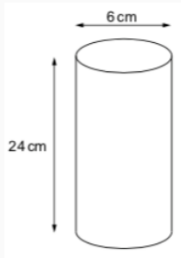


Securing grade 5 – Shape – Perimeter, Area and Volume

Four solid balls are packed in a cylindrical container.



The diameter of each ball is 6 cm.
The cylinder has diameter 6 cm and height 24 cm.

Calculate the volume of unused space in the cylinder.

[The volume V of a sphere is $V = \frac{4}{3}\pi r^3$ where r is the radius.]

The diagram shows a circular pond with a path around it.

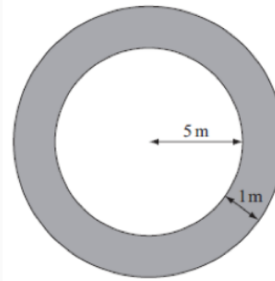


Diagram NOT accurately drawn

The pond has a radius of 5 m.
The path has a width of 1 m.

Work out the area of the path.
Give your answer correct to 3 significant figures.

Frances grows plants in a container.
Each of the 5 faces of the container is made of glass.

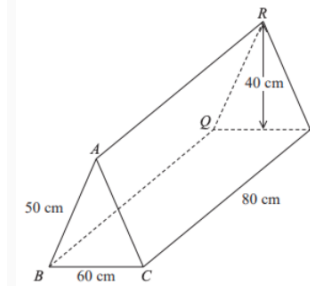


Diagram NOT accurately drawn

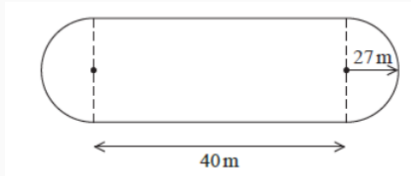
The container is in the shape of a prism.
The cross section of the prism is an isosceles triangle with height 40 cm.

$BC = 60$ cm
 $AB = AC = 50$ cm
 $CP = 80$ cm

Work out the total area of glass needed to make the container.

Securing grade 5 – Shape – Perimeter, Area and Volume

The diagram shows a cycle track.

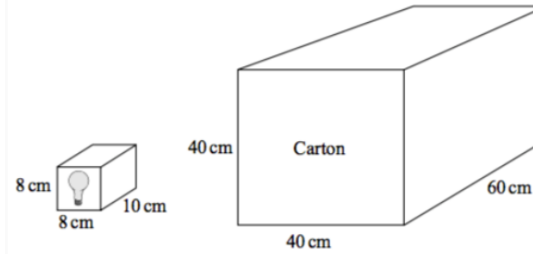


The track has two straight sides each of length 40 m. Each end of the track is a semicircle of radius 27 m.

The diameter of each wheel of Ian's bike is 590 mm. Ian is going to ride his bike around the track once.

Calculate how many **complete** revolutions each wheel of his bike will make.

Diagrams **NOT** accurately drawn



A light bulb box measures 8 cm by 8 cm by 10 cm.
Light bulb boxes are packed into cartons.
A carton measures 40 cm by 40 cm by 60 cm.

Work out the number of light bulb boxes which can completely fill **one** carton.

The diagram shows the floor of a village hall.

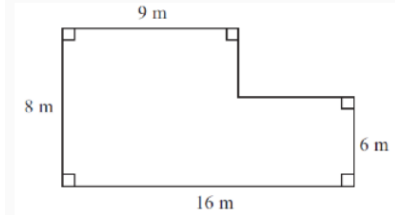


Diagram **NOT** accurately drawn

The caretaker needs to polish the floor.

One tin of polish normally costs £19.
One tin of polish covers 12 m^2 of floor.

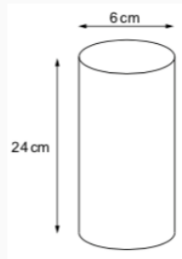
There is a discount of 30% off the cost of the polish.

The caretaker has £130.

Has the caretaker got enough money to buy the polish for the floor?
You must show all your working.

Securing grade 5 – Shape – Perimeter, Area and Volume

Four solid balls are packed in a cylindrical container.



The diameter of each ball is 6 cm.
The cylinder has diameter 6 cm and height 24 cm.

Calculate the volume of unused space in the cylinder.

[The volume V of a sphere is $V = \frac{4}{3}\pi r^3$ where r is the radius.]

$$= 72\pi$$

$$= 226.19\text{cm}^3$$

The diagram shows a circular pond with a path around it.

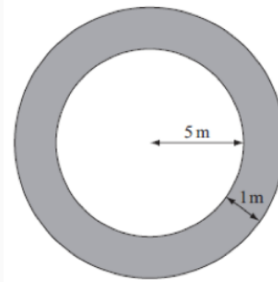


Diagram NOT accurately drawn

The pond has a radius of 5 m.
The path has a width of 1 m.

Work out the area of the path.
Give your answer correct to 3 significant figures.

$$= 11\pi$$

$$= 35.6\text{m}^2$$

Frances grows plants in a container.
Each of the 5 faces of the container is made of glass.

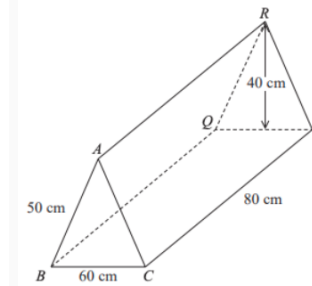


Diagram NOT accurately drawn

The container is in the shape of a prism.
The cross section of the prism is an isosceles triangle with height 40 cm.

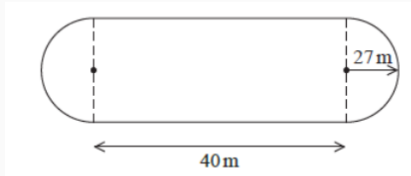
$BC = 60\text{ cm}$
 $AB = AC = 50\text{ cm}$
 $CP = 80\text{ cm}$

Work out the total area of glass needed to make the container.

$$= 15200\text{cm}^2$$

Securing grade 5 – Shape – Perimeter, Area and Volume

The diagram shows a cycle track.



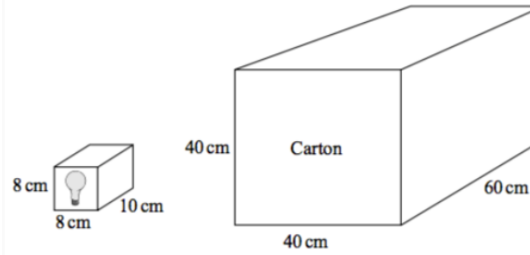
The track has two straight sides each of length 40 m. Each end of the track is a semicircle of radius 27 m.

The diameter of each wheel of Ian's bike is 590 mm. Ian is going to ride his bike around the track once.

Calculate how many **complete** revolutions each wheel of his bike will make.

= 134 full revolutions

Diagrams **NOT** accurately drawn



A light bulb box measures 8 cm by 8 cm by 10 cm. Light bulb boxes are packed into cartons. A carton measures 40 cm by 40 cm by 60 cm.

Work out the number of light bulb boxes which can completely fill **one** carton.

= 150 light bulb boxes

The diagram shows the floor of a village hall.

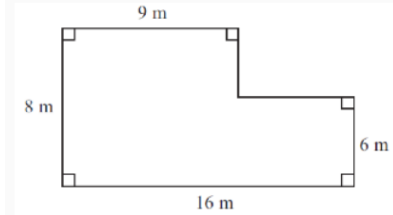


Diagram **NOT** accurately drawn

The caretaker needs to polish the floor.

One tin of polish normally costs £19. One tin of polish covers 12 m² of floor.

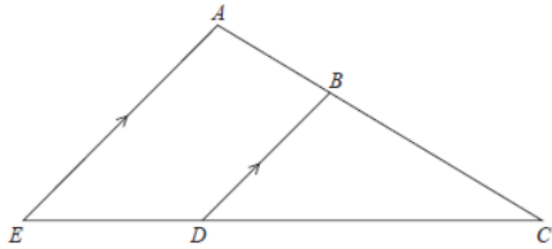
There is a discount of 30% off the cost of the polish.

The caretaker has £130.

Has the caretaker got enough money to buy the polish for the floor? You must show all your working.

= £133 so No he does not have enough money

Securing grade 5 – Shape – Triangles

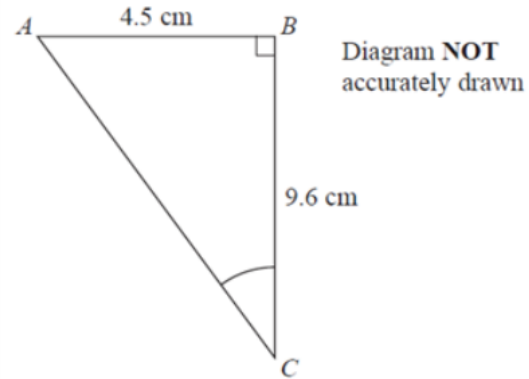


ABC and EDC are straight lines.
 EA is parallel to DB .

$EC = 8.1$ cm.
 $DC = 5.4$ cm.
 $DB = 2.6$ cm.

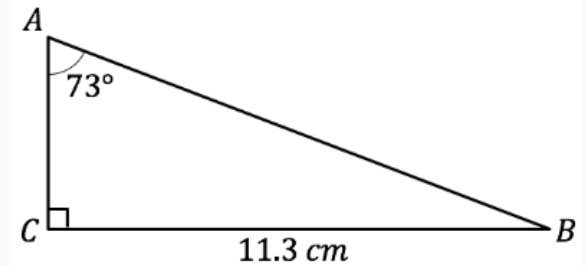
Work out the length of AE .

Work out the size of angle ACB .
Give your answer correct to 1 decimal place.



Work out the length of AC .

Give your answer to 3 significant figures.



Securing grade 5 – Shape – Triangles

A frame is made from wire.

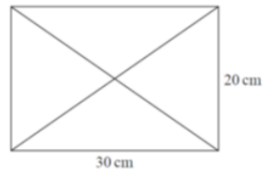


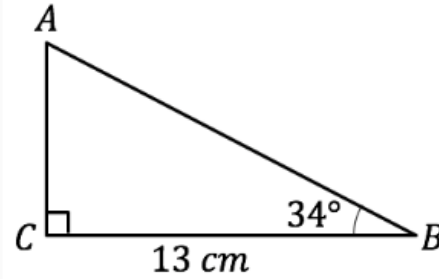
Diagram **NOT** accurately drawn

The frame is in the shape of a rectangle, 30 cm by 20 cm.
The two diagonals of the rectangle are also made from wire.

Calculate the total length of wire needed to make the frame and the diagonals.
Give your answer correct to 1 decimal place.

Work out the length of AC .

Give your answer to 3 significant figures.



The diagram shows a shape with one line of symmetry.

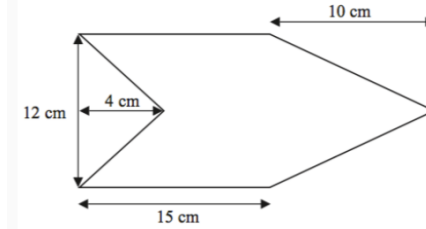
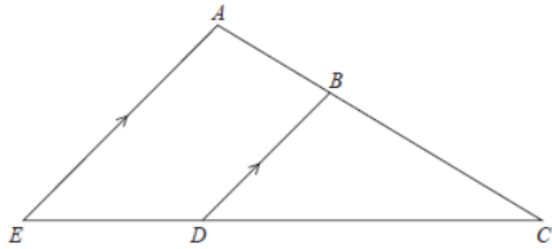


Diagram **NOT** accurately drawn

Work out the area of the shape.

Securing grade 5 – Shape – Triangles



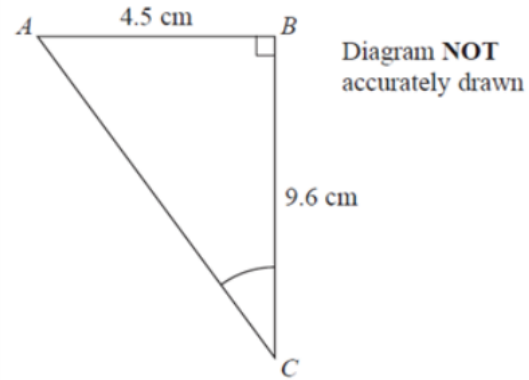
ABC and EDC are straight lines.
 EA is parallel to DB .

$EC = 8.1$ cm.
 $DC = 5.4$ cm.
 $DB = 2.6$ cm.

Work out the length of AE .

= 3.9cm

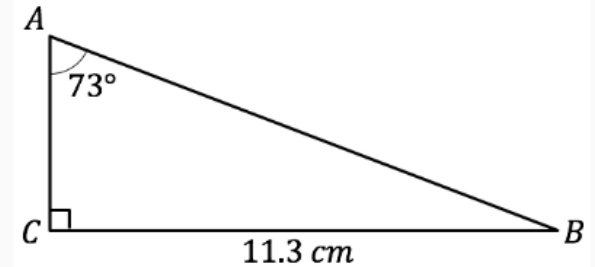
Work out the size of angle ACB .
Give your answer correct to 1 decimal place.



= 25.1°

Work out the length of AC .

Give your answer to 3 significant figures.



= 3.45cm

Securing grade 5 – Shape – Triangles

A frame is made from wire.

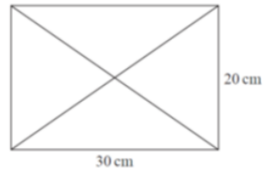


Diagram **NOT** accurately drawn

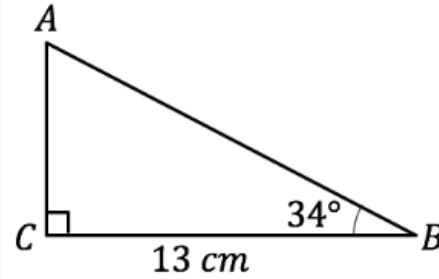
The frame is in the shape of a rectangle, 30 cm by 20 cm. The two diagonals of the rectangle are also made from wire.

Calculate the total length of wire needed to make the frame and the diagonals. Give your answer correct to 1 decimal place.

= 172.1cm

Work out the length of AC .

Give your answer to 3 significant figures.



= 8.8cm

The diagram shows a shape with one line of symmetry.

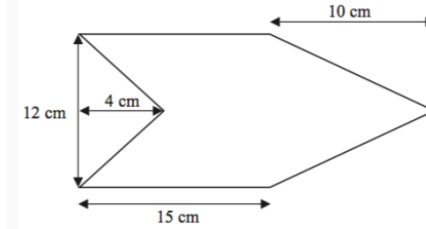


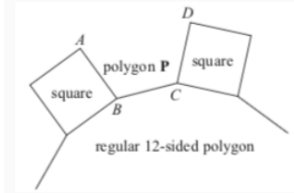
Diagram **NOT** accurately drawn

Work out the area of the shape.

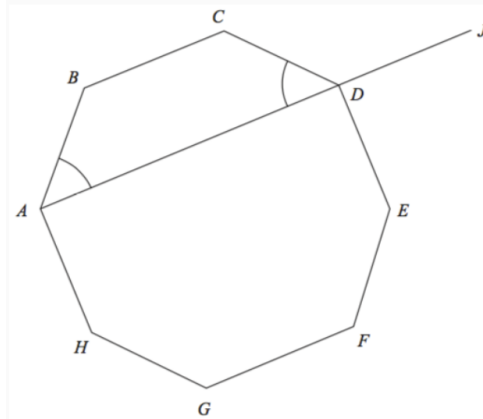
= 216cm²

Securing grade 5 – Shape – Angles

In the diagram, AB , BC and CD are three sides of a regular polygon P .



Show that polygon P is a hexagon.



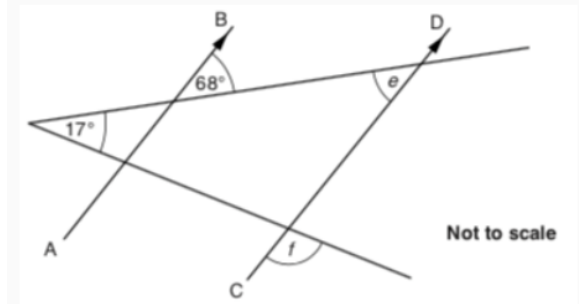
$ABCDEFGH$ is a regular octagon.

ADJ is a straight line.

angle BAD = angle CDA

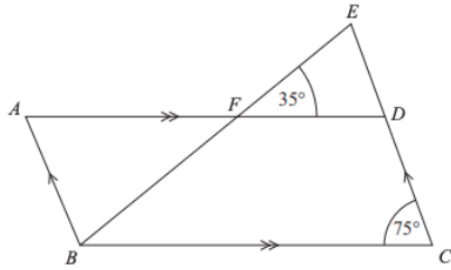
Find the size of angle CDJ

In the diagram AB is parallel to CD .



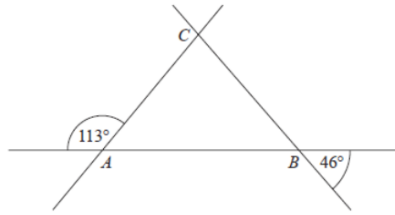
Work out the following angle.

Securing grade 5 – Shape – Angles

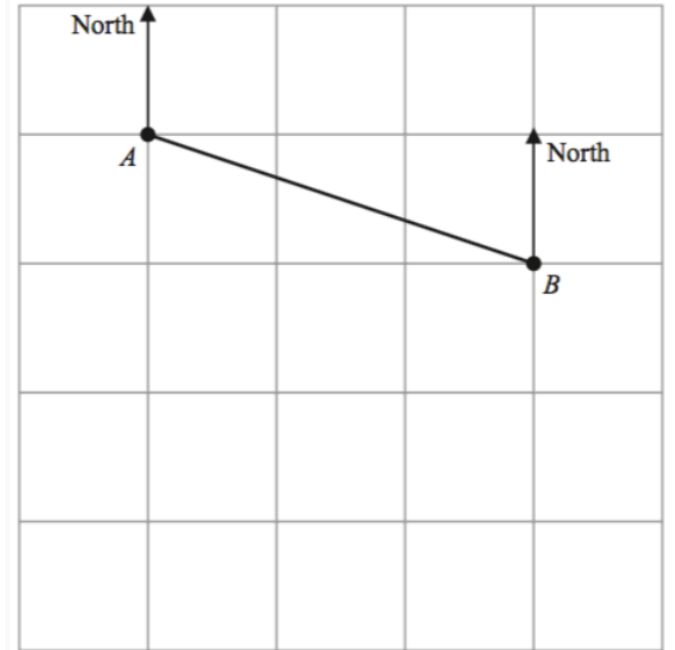


$ABCD$ is a parallelogram.
 EDC is a straight line.
 F is the point on AD so that BFE is a straight line.
 Angle $EFD = 35^\circ$
 Angle $DCB = 75^\circ$
 Find angle ABF .

Here is triangle ABC with each of its sides extended.



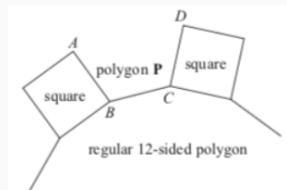
Is the triangle ABC isosceles? Give a reason for each stage of your working.



The diagram shows point A and point B on a map.
 The point C is due south of A .
 The bearing of C from B is 235° .
 The bearing of a point D from B is 168° .
 Find the bearing of B from D

Securing grade 5 – Shape – Angles

In the diagram, AB , BC and CD are three sides of a regular polygon P .



Show that polygon P is a hexagon.

Exterior angle of 12 sided polygon

$$\frac{360}{12} = 30^\circ$$

12

Interior angle of polygon P

$$30 + 90 = 120^\circ$$

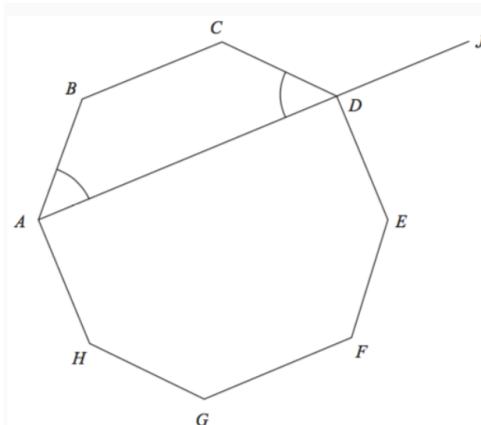
Interior angle of a hexagon

$$\frac{(6-2) \times 180}{6} = \frac{720}{6}$$

6

6

$$= 120^\circ$$



$ABCDEFGH$ is a regular octagon.

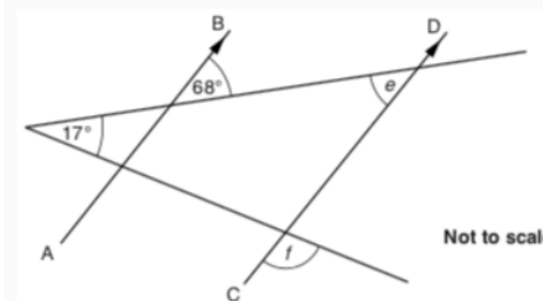
ADJ is a straight line.

angle $BAD =$ angle CDA

Find the size of angle CDJ

$$= 135^\circ$$

In the diagram AB is parallel to CD .

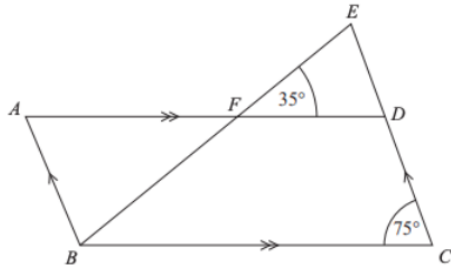


Work out the following angle.

$$e = 68^\circ$$

$$f = 95^\circ$$

Securing grade 5 – Shape – Angles



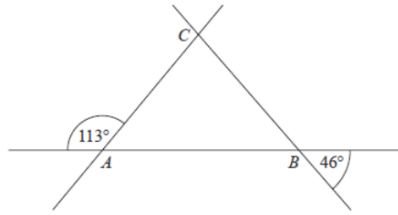
$ABCD$ is a parallelogram.
 EDC is a straight line.
 F is the point on AD so that BFE is a straight line.

Angle $EFD = 35^\circ$
 Angle $DCB = 75^\circ$

Find angle ABF .

$ABF = 70^\circ$

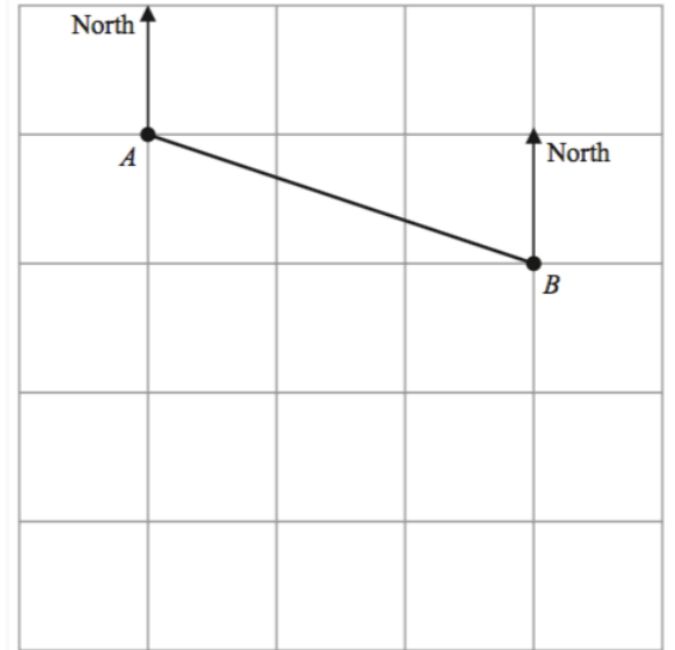
Here is triangle ABC with each of its sides extended.



Is the triangle ABC isosceles? Give a reason for each stage of your working.

$ABC = 46^\circ$ Vertically opposite angles are equal
 $CAB = 67^\circ$ Angles on a straight line equal 180 degrees
 $ACB = 67^\circ$ Angles in a triangle equal 180 degrees

Yes it is isosceles as the base angles are equal.



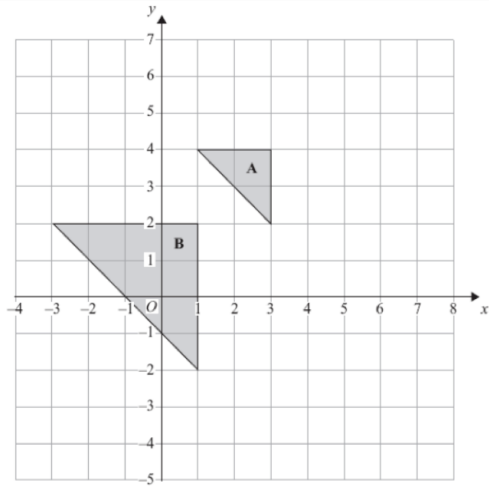
The diagram shows point A and point B on a map.
 The point C is due south of A .
 The bearing of C from B is 235° .

The bearing of a point D from B is 168° .

Find the bearing of B from D

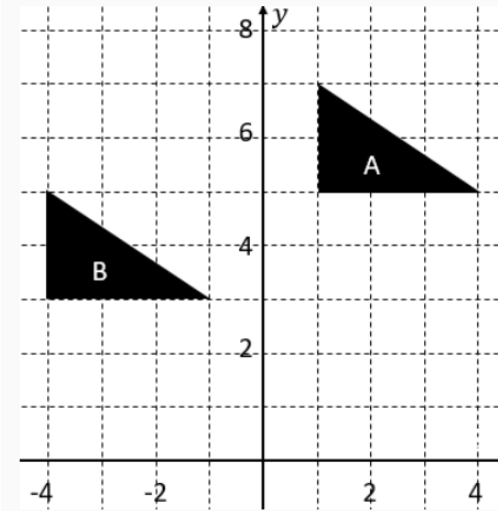
$e = 348^\circ$

Securing grade 5 – Shape – Transformations and Vectors



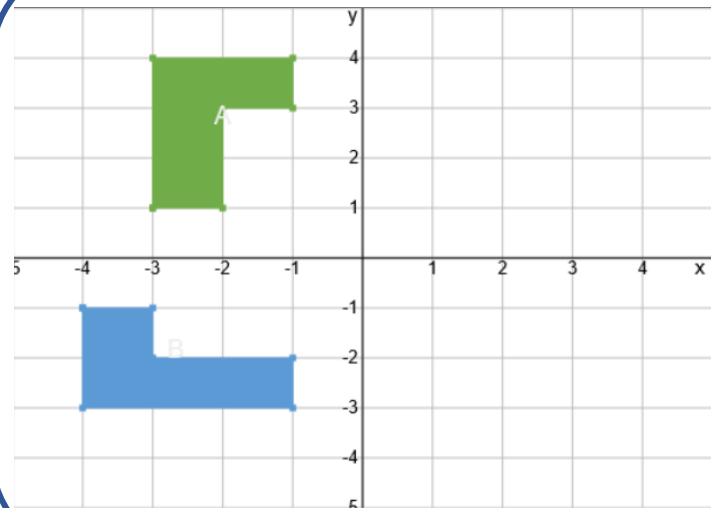
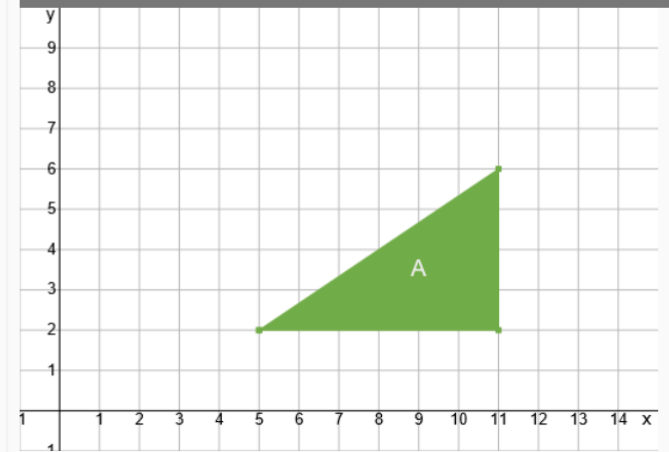
Triangle A and triangle B are drawn on the grid.
Describe fully the single transformation which maps triangle A onto triangle B.

Describe the transformation from A to B:

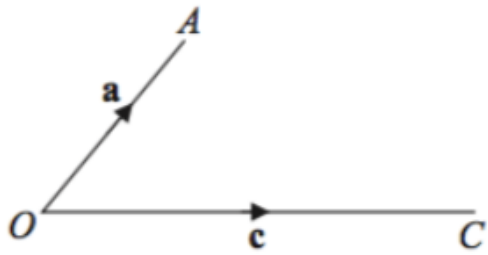


Enlarge shape A by scale factor $\frac{1}{2}$ about the point (5, 8).

Click/Press each point of your polygon.

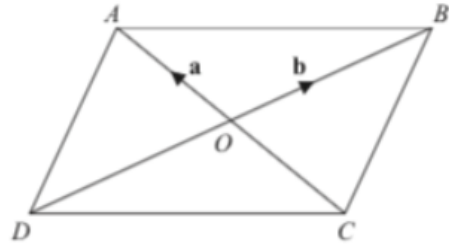


- a) Rotate shape B by 90° anticlockwise from the origin
- b) Reflect shape A in the line $x = 1$



In the diagram $\vec{OA} = \mathbf{a}$ and $\vec{OC} = \mathbf{c}$.

Find \vec{CA} in terms of \mathbf{a} and \mathbf{c} .



$ABCD$ is a parallelogram.
The diagonals of the parallelogram intersect at O .

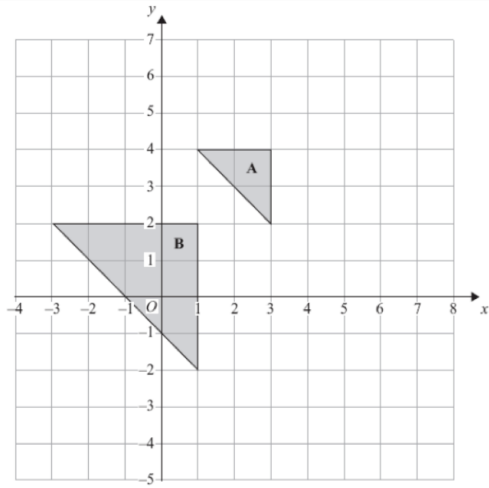
$\vec{OA} = \mathbf{a}$ and $\vec{OB} = \mathbf{b}$

Find, in terms of \mathbf{a} and \mathbf{b} , the vector \vec{AB}

Vector $\mathbf{p} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$ and vector $\mathbf{q} = \begin{pmatrix} -2 \\ 2 \end{pmatrix}$

Calculate $\mathbf{p} + \mathbf{q}$

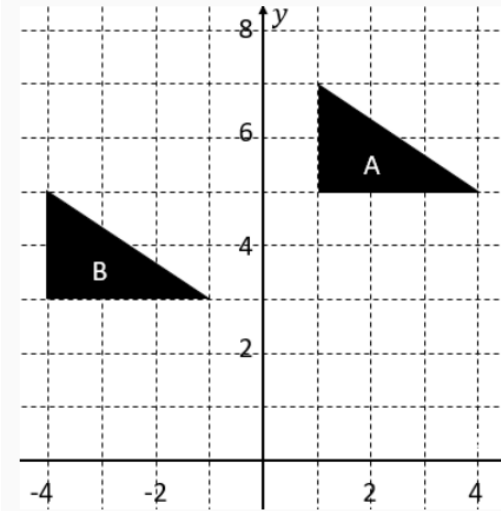
Securing grade 5 – Shape – Transformations and Vectors



Enlargement
Scale factor 2
From the point (5,6)

Triangle A and triangle B are drawn on the grid.
Describe fully the single transformation which maps triangle A onto triangle B.

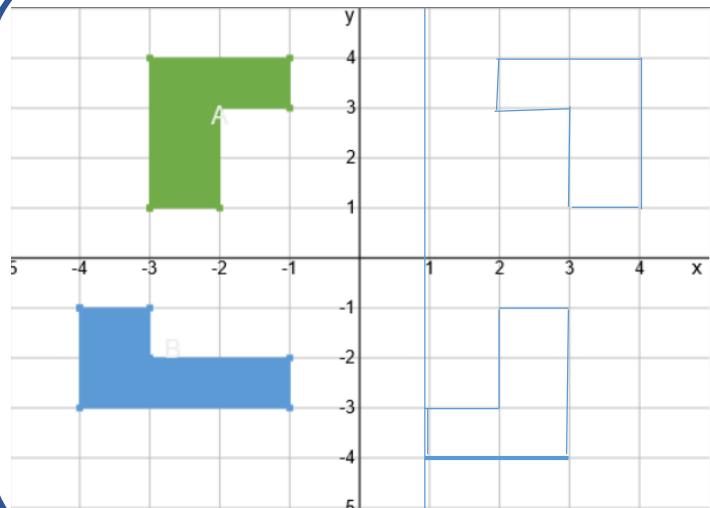
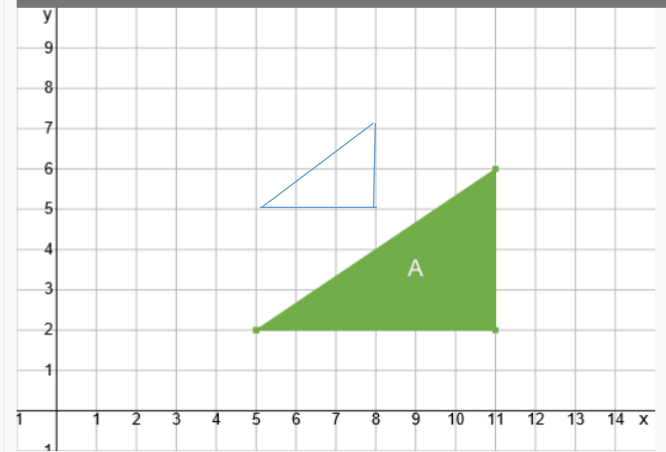
Describe the transformation from A to B:



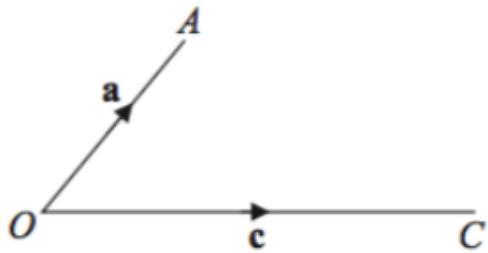
Translation
-5
-2

Enlarge shape A by scale factor $\frac{1}{2}$ about the point (5, 8).

Click/Press each point of your polygon.



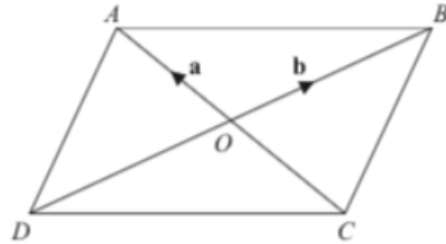
- a) Rotate shape B by 90° anticlockwise from the origin
- b) Reflect shape A in the line $x = 1$



In the diagram $\vec{OA} = \mathbf{a}$ and $\vec{OC} = \mathbf{c}$.

Find \vec{CA} in terms of \mathbf{a} and \mathbf{c} .

$$= -\mathbf{c} + \mathbf{a}$$



$ABCD$ is a parallelogram.
The diagonals of the parallelogram intersect at O .

$\vec{OA} = \mathbf{a}$ and $\vec{OB} = \mathbf{b}$

Find, in terms of \mathbf{a} and \mathbf{b} , the vector \vec{AB}

$$= -\mathbf{a} + \mathbf{b}$$

Vector $\mathbf{p} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$ and vector $\mathbf{q} = \begin{pmatrix} -2 \\ 2 \end{pmatrix}$

Calculate $\mathbf{p} + \mathbf{q}$

1
1